

Source: **Cohere Technologies**  
Title: **PRACH Preamble Format Design**  
Agenda item: **5.1.1.4.1**  
Document for: **Discussion/Decision**

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## 1. Introduction

In [1] the Root Hamming windowed repetition Zadoff-Chu sequence was presented, and was shown to greatly improve resilience to Doppler. In this submission, we demonstrate that the Doppler resilience of repetition M-sequences can also be improved through the application of a window.

## 2. Root Hamming Windowed M sequence

We propose a 3x repetition M-sequence with a Root-Hamming window. Let  $N$  denote the length of the M-sequence in baseband. Then,  $M = 3N$  is the length of the final sequence. Denote the sequence by  $p$ , then:

$$p[m] = w_r[m] s[\text{mod}(m, N)], \text{ for } m = 0, 1, \dots, M - 1$$

Where  $w_r$  denotes the Root-Hamming window, and  $s$  denotes a M-sequence. The Root-Hamming window is defined below:

$$w[m] = \sqrt{0.54 - 0.46 \cos(2\pi m / (M - 1))} \text{ for } m = 0, 1, \dots, M - 1$$

## 3. Simulation results/Discussion

The PRACH performance of a repetition M-sequence was compared with and without a Root-Hamming window. In the simulations, a unit power amplifier was used for all sequences, so effects of PAPR are included. The channel parameters are given in table 1. The sequence parameters are given in table 2.

**Table 1: Simulation Parameters**

<b>Channel model</b>	<b>CDL-C (100 ns scaling)</b>
<b>MIMO order</b>	<b>1 x 1 x 2</b>
<b>UE speed</b>	<b>250, 500 km/h</b>
<b>Carrier frequency</b>	<b>4 GHz</b>
<b>Timing offset</b>	<b>0-100 <math>\mu</math>s</b>
<b>Frequency offset</b>	<b>0.1 ppm at UE, 0.05 ppm at TRP</b>
<b>PRACH bandwidth</b>	<b>1.08 MHz</b>

**Table 2: Sequence Parameters**

<b>Symbols in M sequence</b>	<b>255</b>
<b>Subcarrier spacing</b>	<b>3.75 kHz</b>
<b>Repetitions of M sequence</b>	<b>3</b>
<b>Total number of symbols</b>	<b>765</b>

Figure 1 compares the missed detection rate of the two sequences at 500 km/h. Note that the application of the Root-Hamming window gives both an SNR gain and removes the error floor.

- **SNR Gain:** the blue line is shifted 0.5 – 1.0 dB to the left of the red line.
- **Error floor:** the red line asymptotes slightly below  $10^{-3}$  missed detection rate, while the blue line achieves a missed detection rate below  $10^{-4}$ .

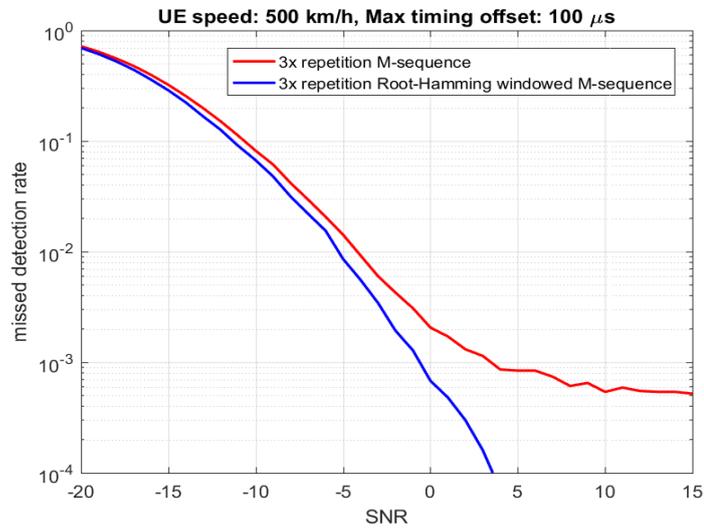


Figure 1: Miss detection probability; 500 km/h; maximum timing offset: 100  $\mu$ s.

Figure 2 compares the missed detection rate of the two sequences at 250 km/h.

- **SNR Gain:** the blue line is shifted 0.5 – 6.0 dB to the left of the red line.

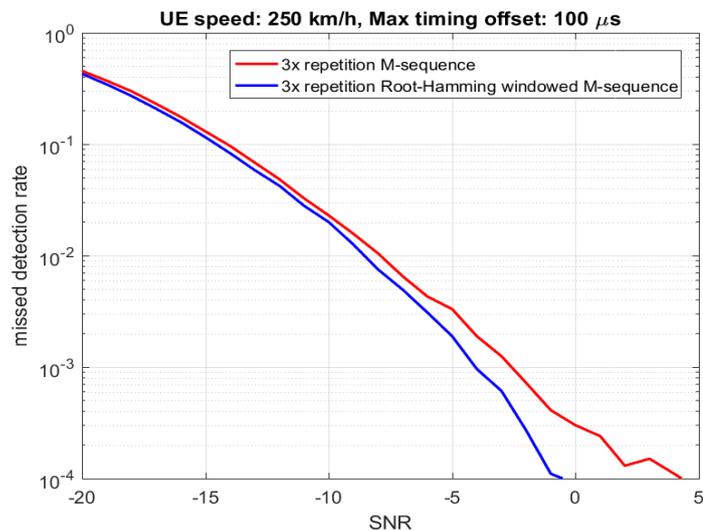


Figure 2: Miss detection probability; 250 km/h; maximum timing offset: 100  $\mu$ s.

### **3.1 Discussion**

*Observation 1: The application of windowing to repetition PRACH sequences improves resilience to Doppler.*

*Observation 2: For 3x repetition sequences the Hamming window gives excellent performance.*

*Observation 3: For different repetitions, other windows will be optimal.*

*Proposal 1: For the high speed and large cell case, for repetition PRACH sequences the use of windowing should be further studied.*

### **4. References**

- [1]. R1-1705458, "PRACH Design", 3GPP RAN1 #88bis, Spokane, WA, USA, April 2017.